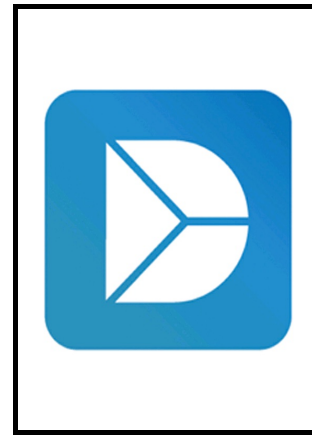# Author's Accepted Manuscript

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Cite this article as: Modupe Elizabeth Ojewumi, Kayode Gbolahan Oyeyemi, Moses Eterigho Emetere and Joshua Olusegun Okeniyi, Data on the rheological behavior of cassava starch paste using different models, *Data in Brief,* https://doi.org/10.1016/j.dib.2018.06.112

Data on the rheological behavior of cassava starch paste using different models

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Abstract

Proper selection of rheological models is very important in flow characterization. These models are often used to evaluate parameters that help in the characterization of food samples. Rheological models also provide flow predictions for extreme conditions where the flow nature of the fluid cannot be determined, Hence the need for appropriate selection of rheological models. The principal aim of this study is to suggest a rheological model that best characterize the rheological behavior of native cassava starch and to determine the effect of state variables like temperature and concentration on the accuracy of rheological models. Five rheological models (i.e. Herschel-Bulkley model, Robertson-Stiff model, Power-law model, Bingham plastic model and Prandtl-Eyring model) were selected for this study and these models were modified into statistical models by the inclusion of the error variance (ε). The least-square method was used in evaluating the various model parameters for each model. From this study, it was seen that the Herschel-Bulkley model and the Robertson-Stiff model most accurately described the rheological patterns in cassava starch production. The sensitivity analysis of the different rheological models also shows that the accuracy of the Herschel-Bulkley model, Robertson-Stiff model and Power-law model is not significantly affected by variations in temperature and concentration of the cassava starch. However, it was observed that the Bingham plastic model and Prandtl-Eyring model gave less accurate predictions at higher concentration and lower temperature respectively. A lot of the industrially accepted models such as the Bingham plastic model may not necessarily be the best model for characterization cassava starch production as shown in this study, hence rheological model optimization is recommended for further study.

Specifications Table

Subject area	*Chemical Engineering*
More specific subject area	*Rheology*
Type of data	*Table, graph, figure*
How data was acquired	*Laboratory and Modelling*
Data format	*Raw, filtered and Analyzed data*
Experimental factors	*Statistical modelling was used.*
Experimental features	*Five rheological models (i.e. Herschel-Bulkley model, Robertson-Stiff model, Power-law model, Bingham plastic model and Prandtl-Eyring model) were*

	selected for this study and these models were modified into statistical models by the inclusion of the error variance (ε).
Data source location	*Ogun State, Nigeria*
Data accessibility	*Data set is with this article*

Value of the data

- *The dataset will help to investigate the rheological properties of cassava starch.*
- *Data will assist in developing best model for cassava starch characterization using Statistical optimization of five rheological models.*
- *Effect of state variables like temperature and concentration on the accuracy of rheological models will be determined using the dataset.*

1. Data

Dataset provided in this work revealed that investigations of rheological measurement does not only involve flow behaviour of liquids, but also on solids deformation behaviour. This research work examines the rheological behavior of native cassava starch as well as the factors affecting the rheological behavior of cassava starch. Rheological characterization using rheological models as well as sensitivity analysis of these models were also examined. The model specification of this project was limited to models that relate shear stress to shear rates.

Rheological properties measurement of materials must be subjected to a precised, controlled and quantifiable strain over a given time and the material parameters such as modulus, hardness, viscosity, stiffness, strength or toughness are determined by considering the subsequent forces [1,2]. Rheological measurements shows how materials react under defined conditions- its performance during practical processing such as mixing, sheeting, binding, baking and proofing [3-8]. In recent times, the utilization of starch has grown from mere domestic use to highly intensive industrial use. It is used either in its native form or after chemical or physical modifications. Starch is not only a basic food in the human or animal diet; it is also broadly used as raw material in the food industry as well as textile, paper and other industries. Starch is mostly in granular form and has different shapes and sizes depending on its botanical source [9]. Starch is a glucose polymer comprising macromolecules of amylopectin and amylose [10,11]. Texture is an essential factor in consumers' perception of food quality and has been studied for several years. Rheological profiling offers an unparalleled insight into the textural, handling, stability and appearance characteristics of starch-based products. Starch functions by building structures in a formulation or recipe. It is the presence of such structures that imparts texture, handling, suspending and appearance attributes to a formulation. The importance of rheological models in the characterization of food behavior cannot be over emphasized. Rheological models are used, together with experimental data, to estimate values of parameters that help characterize the rheological behavior of a food samples. One such model is that of Herschel Bulkley model which has been used extensively to characterize foods that exhibit yield stress. Rheological models sometimes called Flow models, this can also be used to derive expressions for volumetric flow rates and velocity profiles in tube and channel flows, and in the analysis of heat transfer phenomenon. Quite a number of these models can be encountered in rheology literature [12]. The applied force is essential for letting the fluid to flow

because of fluid friction and this friction has to be overcome before the fluid can flow. Rheological models give a surmised description of fluids by communicating the mathematical relationship between shear stress and shear rates [13]. Mathematical model is regarded as a decision tool that assists decision makers in effectively dealing with complex issues such as rheology and oil spillage on soil surfaces. Such information can be key in decision-making for further experiments and can enable the development of robust and reliable protocols for chemical synthesis, analytical methods or biological assays [14].

There are different models used to measure rheological properties. This research work used models such as power law model, Herschel-Bulkley model, Bingham Plastic model, Prandtl-Eyring model and Robertson-Stiff model. This work did not explain all the available testing methods and general reviews of rheology [15-17]. A lot of work has been done on rheological testing of foods [12,18-21] and cereal products [22-25].

2. Experimental Design, Materials and Methods

Cassava starch tubers were purchased from the local market.

2.1. Flow properties measurement

The sample solution was prepared by dissolving the required quantity based on the required composition needed. 20.00, 30.00, 40.00, 50.00 g of the cassava starch powder was carefully weighed with the aid of a weighing balance and was dissolved in a 400 ml of clean warm water inside a 600 ml beaker until a solution was formed so as to make a reconstituted product. The sample was transferred into the temperature controlled water bath in order to form an aqueous gel which was later placed in a cold water bath (4^oC) medium so as to facilitate the drop in the temperature of the gel to 70, 60, 50, 40 and finally 30^oC. The Ofite viscometer was used in determining the flow characteristics in terms of shear rate and shear stress. A bob of radius 1.8415cm was used at speeds of 3, 6, 30, 60,100,200,300 and 600 rpm to effectively determine the dial deflection so as to evaluate the shear stress and shear strain.

2.2. Statistical Evaluation of Rheological models

The least square method was used in evaluating model parameters for each model based on the data obtained from the rheological experiment. This method was chosen due to the following assumptions:

   I.   *The scatter follows a Normal distribution*

   II.   *Errors are random errors that are independent and identically distributed with mean of zero and variance, σ^2.*

Considering P number of data points ($\tau_i, \gamma i$), least-square is expressed mathematically in equation 1 below.

$$RSS\ (\mu) = \sum_{i=1}^{P}(\tau i - f(\gamma i, \mu))^2 = \in^2 \qquad (1)$$

RSS (μ) representing the residual sum of squares.

∈ represents random errors.

μ representing the value(s) of model parameters that gives minimum RSS (also called Least-Square estimators). μ has to be determined such that RSS (μ) will be minimum. Therefore, for the sum of squares to be minimum the partial differential $\frac{\delta RSS\ (\mu)}{\delta\mu}$ = **0.** The experimental data were fitted to the models using the method above on MATLAB 8.0 to obtain model curve-fits, their corresponding model parameters, residual plots, RMS and RSS values which are necessary for model optimization

2.3. Preparation of starch from the cassava roots

The cassava tubers purchased were peeled and washed thoroughly. After which the roots were crushed and grinded in the market using a local grinder. The grinded cassava was then soaked in water and screened by passing it through a screening bag to remove the shafts and other unnecessary products. The filtrate was then allowed to settle for a period of one and a half days, after which the solution was dewatered by a simple process of decantation. The resulting product was starch of a moisture content of 36.5%.

2.4. Determination of moisture content of starch

The moisture content was evaluated using [26-28]. 2.00g of the starch was weighed into two different empty Petri dishes. The dishes were then placed into an oven at $150^o C$ for 4 hrs. The dried starch was immediately transferred into a desiccator until it cooled, and it was then weighed. The weight-loss expressed as a percentage was taken as the percent moisture. The result was obtained as the average of the two independent determinations from both samples.

$$\%\ Moisture = \frac{W1 - W2}{W3} X\ 100\% \qquad (2)$$

Where:

W1= weight of sample ± Petri dish before drying (g)

W2=Weight of sample ± Petri dish after drying (g)

W3=Weight of sample (g)

3. Rheological experiment

20.00, 30.00, 40.00, 50.00 g of the cassava starch was carefully weighed with the aid of a weighing balance and was dissolved in a 400 ml of clean warm water inside a 600 ml beaker until a solution was formed so as to make a reconstituted product. The sample was transferred into the temperature controlled water bath in order to form an aqueous gel which was later preferably placed in a cold water bath (4⁰C) medium so as to facilitate the drop in the temperature of the gel to 70, 60, 50, 40 and finally 30⁰C. The Ofite viscometer was used in determining the flow characteristics in terms of shear rate and shear stress. A bob of radius 1.8415cm was used at speeds of 3, 6, 30, 60,100,200,300 and 600 rpm to effectively determine the dial deflection so as to evaluate the shear stress and shear strain.

3.1. Determination of gelatinization temperature

A thermometer was inserted into the beaker before placing it into the water bath. The solution was stirred continuously until its colour became milky and thickened. This is the gel point and the temperature at this point was read off as the gelatinization temperature. This was done for each starch concentration.

4. Rheological model optimization

Residual mean squares, Residual sum of squares and Coefficient of determination used as statistical tools to evaluate the error variance for each model.

(i) $$RMS = \frac{RSS}{Degree\ of\ freedom} = \frac{RSS}{N-M}$$

RMS representing the residual mean squares

N representing the number of data

M representing the number of parameters in a model

(ii) $$R\text{-squared} = 1 - \frac{RSS}{TSS}$$

RSS representing the Residual sum of squares.

TSS representing the Total sum of squares.

(iii) $$Residuals = \tau - \tau'$$

τ representing the observed values.

τ' representing the predicted values.

The residual plot is a graph showing the residuals vs the independent variable (γ).

4.1. Model curve-fits and their corresponding residual plot analysis

1. Bingham plastic ($\tau = \tau_o + \mu_p \gamma$)

Experimental data was fitted into the Bingham plastic model and the corresponding model parameters were evaluated. Figure 1 represents the fitted model while Figure 2 represents the corresponding residual plot. The model parameters τ_o and μ_p were found to be

τ_o =9.8566Ibf/100ft^2 (Yield stress)
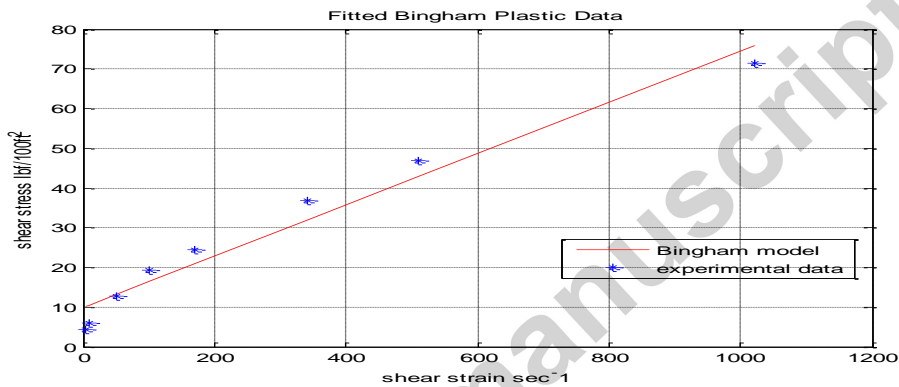μ_p =0.0647Ibf.s/100ft^2 (Plastic viscosity)

Fig. 1. Experimental data and fitted Bingham plastic flow curve

From the above plot it can be clearly seen that the Bingham plastic model gives a very poor fit to the experimental data.
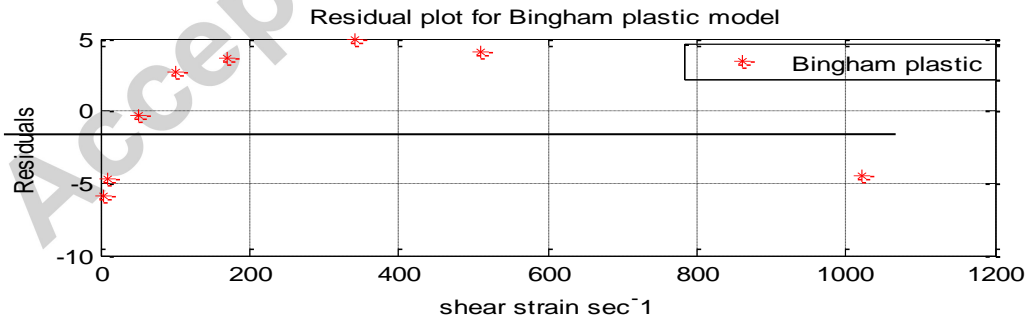

Fig. 2. Residual plot of the Bingham plastic model

Observations from the residual plot show that the residual do not follow a random distribution or pattern and almost all the residuals are far away from the reference line (residual = 0) indicating a poor fit. Residuals between shear rate of 102.18 s^{-1} to 510.9 s^{-1} lie above the reference line (residual = 0), that is there are positive residuals while the rest of the residual point lie below the reference line indicating negative residuals.

2. Power-law model (τ = K γ ^{n})

The power law model gave a better fit than the Bingham plastic model as illustrated in Figure 3, which shows the fitted power-law model. The model parameter K,**γ**, n were evaluated and found to be:

K=1.2831Ibf.s/100ft^2 (Consistency index) which depicts the thickness of the fluid.

n=0.5789 (Flow index) indicates that the fluid is Pseudo-plastic i.e. n<1

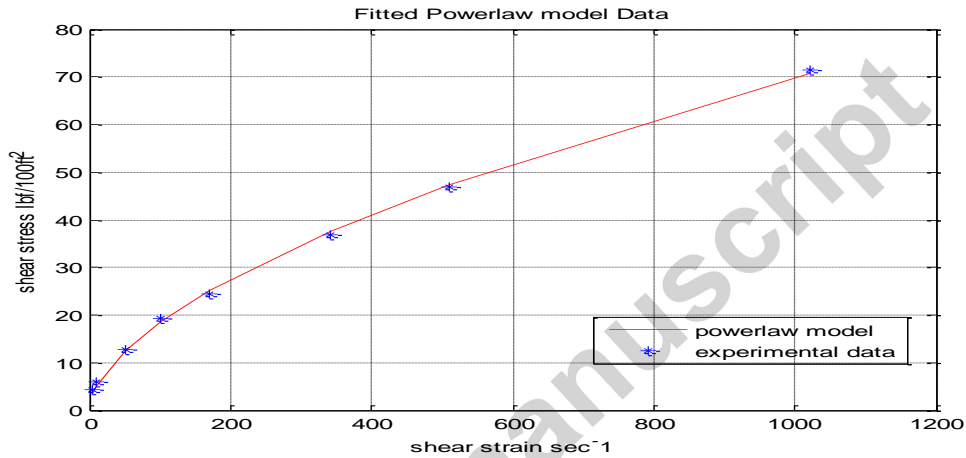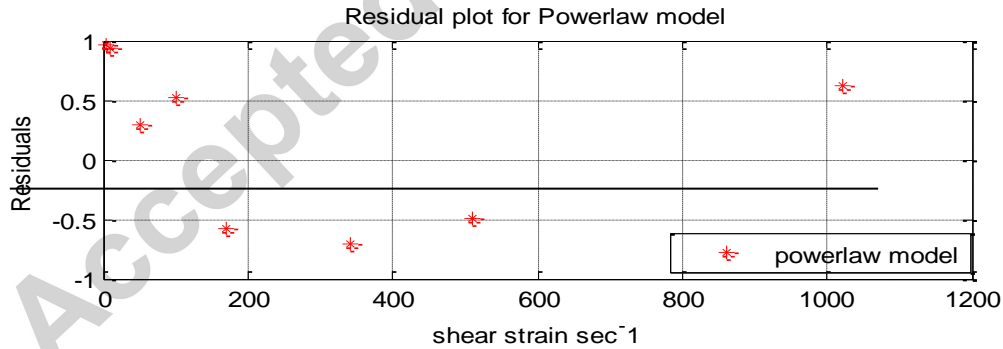**Fig. 3. Experimental data and fitted Power-law flow curve**

Fig. 4. Residual plot of the Bingham plastic model

Figure 4 illustrates the residual plot of the power-law model. It can be observed from the plot that the scatter follow a random distribution along the entire range of shear rates. It can also be seen that compared to the Bingham plastic model the residual points of the power-law model are closer to the reference line (residual= 0). Both points indicating that the model gives a good fit.

3. Herschel Bulkley model ($\tau = \tau_o + K \gamma^n$)

The Herschel-Bulkley model which is just a modification of the power-law model by the inclusion of the yield stress (τ_o). From Figure 5, it can be observed that the Herschel-Bulkley model gave a very good fit with model parameters:

$\tau_o = 1.6825 \text{Ibf}/100\text{ft}^2$ (Yield stress)

$K = 0.9893 \text{Ibf.s}/100\text{ft}^2$ (Consistency index)

$n = 0.6138$ (flow index)

Although the fitted flow curves of both the power-law and the Herschel-Bulkley look alike, dissimilarities can be seen in their residual plots (see Figure 6).
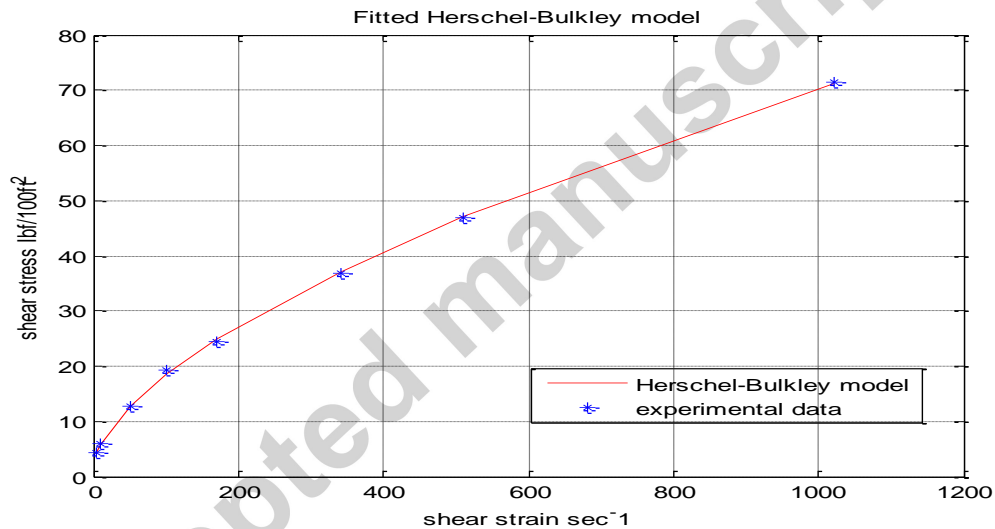

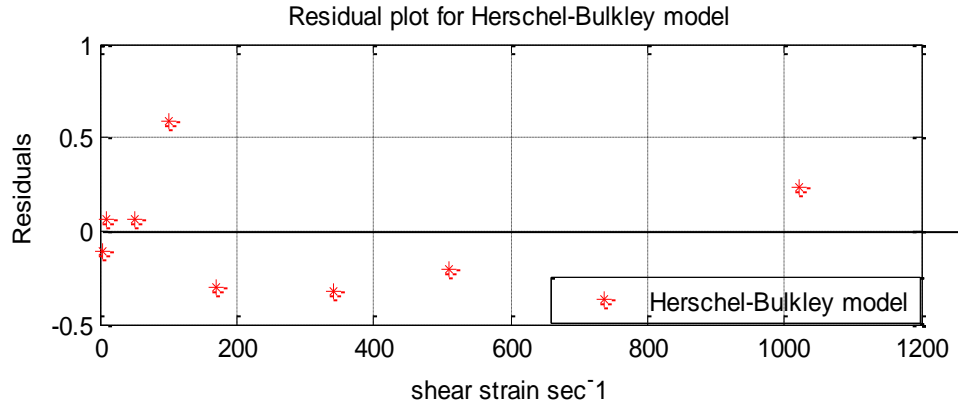**Fig. 5. Experimental data and fitted Herschel-Bulkley flow curve**

Fig. 6. Residual plot of the Herschel-Bulkley model

Figure 6 shows the residual plot of the Herschel-Bulkley model. It can be ascertained from the plot that the scatter follow a random distribution along the entire range of shear rates. It can also be seen that compared to the Bingham plastic model and the power-law model, the residual points of the Herschel-Bulkley model are closer to the reference line (residual= 0). Also since the Herschel-Bulkley model gave better predictions than the power-law model throughout the entire range of shear rate (especially at higher shear rates), the Herschel-Bulkley can therefore be depended upon to give accurate predictions at higher shear rates outside the range used in this project.

4. Robertson-Stiff model ($\tau = A\,(\gamma_o + \gamma)^B$)

Robertson-Stiff model is quite different from the other models being the only model with the yield shear rate (γ_o). The model parameters were evaluated to be:

A= 1.1314Ibf.$s^{0.4026}$/100ft^2 (the unit of A depends on the value of B)

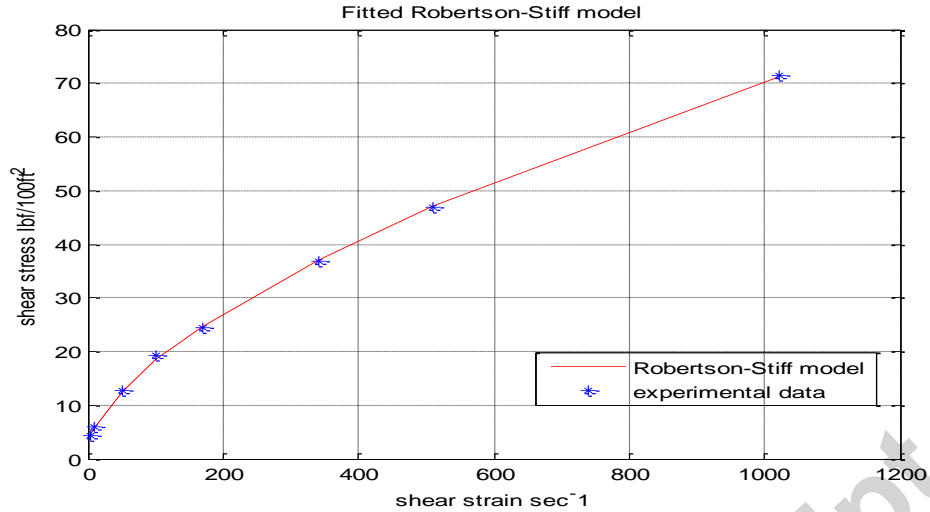B= 0.5974

γ_o= 5.1561s^{-1}

Fig. 7. Experimental data and fitted Robertson-Stiff flow curve

Although the fitted flow curves for Robertson-Stiff, power-law and the Herschel-Bulkley model all look similar, dissimilarities can be seen in their residual plots (see Figure 8).
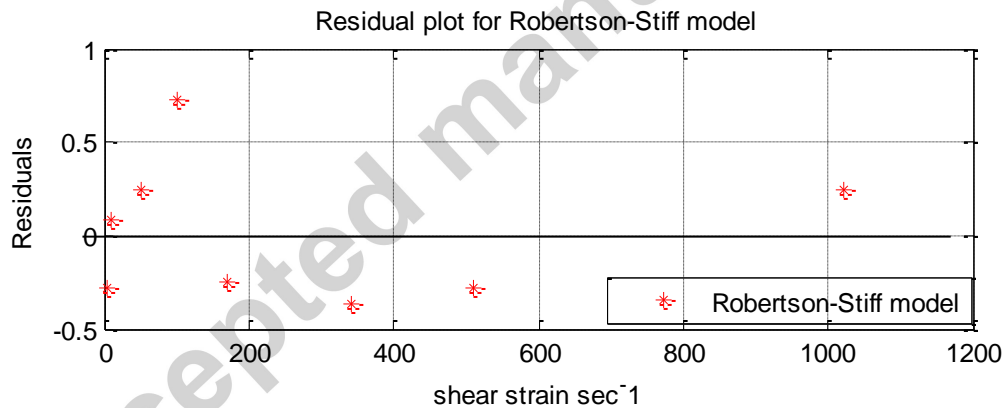

Fig. 8. Residual plot of the Robertson-Stiff model

From Figure 8 it can be seen that the scatter of the residual plot follows a random distribution along the entire range of shear rates. The residual points are also close to the reference line (residual=0). The model also gives a good fit.

5. Prandtl-Eyring model (τ =Asinh^{-1}($^{\gamma}/_{B}$)

Figure 9 represents the fitted flow curve for the Prandtl-Eyring model. The model parameter A and B where estimated thus:

A=26.7032

B=159.0655

Although it can be observed from the fitted flow curve that the model does not fit the data accurately, this model however fits better than the Bingham plastic model.
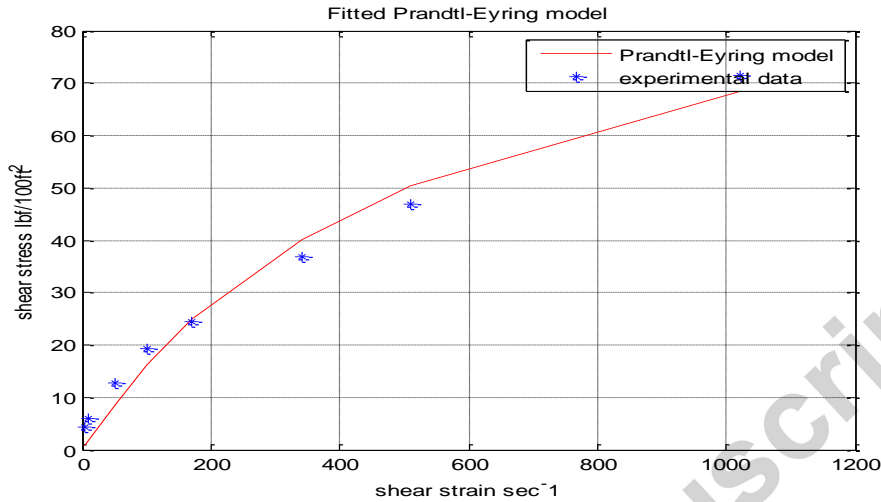

Fig. 9. Experimental data and fitted Prandtl-Eyring flow curve

Figure 10 shows the residual plot for the Prandtl-Eyring model. From this plot it can be seen that the scatter are not randomly distributed, and the residual points are far away from the reference line (residual=0). This suggests that the model does not accurately give a good fit. However in comparison with the Bingham plastic model, the residual points of the Prandtl-Eyring model are closer to the reference line (residual=0). This indicates that the Prandtl-Eyring model gives a much better fit than the Bingham plastic model.
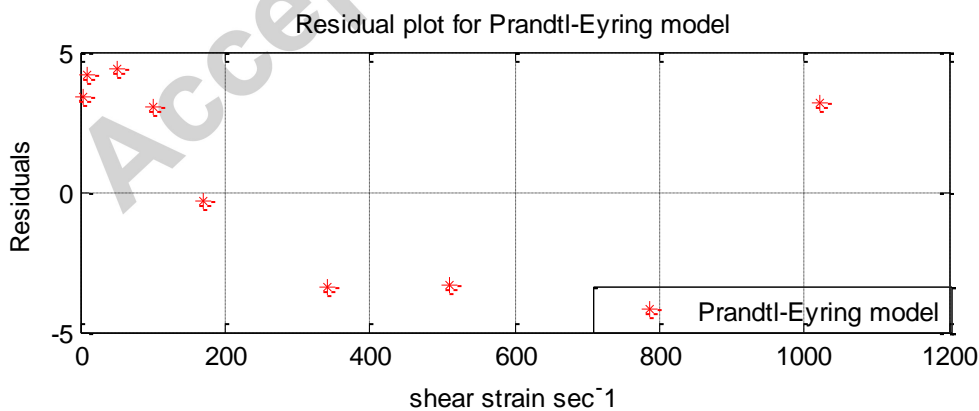

Fig. 10. Residual plot of the Prandtl-Eyring model

5. Sensitivity analysis

Sensitivity analysis was carried out on each model using the multiple-factor-at-a-time approach (MFAT). The influence of state variables like concentration and temperature on the accuracy of the Bingham Plastic model was examined. Figure 14 shows the result when the sensitivity analysis at constant concentration and varied temperature was carried out on the Bingham plastic model.

Table 1

Result summary of Rheological Optimization using Least-Square method at 700C and 50g/L.

Model	RSS $Ibf^2/100ft^4$	RMS $Ibf^2/100ft^4$	R^2	Evaluated parameters
Bingham Plastic	138.2484	23.0414	0.9626	$\tau_o = 9.8566\ Ibf/100ft^2$ $\mu_p = 0.0647\ Ibf.s/100ft2$
Power-law	3.6559	0.6093	0.999	$K = 1.2831\ Ibf.s/100ft^2$ $n = 0.5789$
Herschel-Bulkley	0.661	0.1322	0.9998	$\tau_o = 1.6825\ Ibf/100ft^2$ $K = 0.9893\ Ibf.s/100ft^2$ $n = 0.6138$
Robertson-Stiff	1.0001	0.2	0.9997	$A = 1.1314\ Ibf.s^{0.4026}/100ft^2$ $B = 0.5974$ $\gamma o = 5.1561 s^{-1}$
Prandtl-Eyring	89.9357	14.9893	0.9757	$A = 26.7032$ $B = 159.0655$

Table 2

Sensitivity analysis of the Bingham plastic model at constant concentration

	Bingham plastic model			50g/L concentration
Temperature ^0C	RSS $Ibf^2/100ft^4$	RMS $Ibf^2/100ft^4$	R^2	Evaluated parameters
70	138.2484	23.0414	0.9626	$\tau_o = 9.8566\ Ibf/100ft^2$ $\mu_p = 0.0647\ Ibf.s/100ft^2$
60	181.5753	30.26255	0.9596	$\tau_o = 9.8566\ Ibf/100ft^2$ $\mu_p = 0.0647\ Ibf.s/100ft^2$
50	253.0253	42.17088333	0.9555	$\tau_o = 9.8566\ Ibf/100ft^2$ $\mu_p = 0.0647\ Ibf.s/100ft^2$
40	264.9318	44.1553	0.9621	$\tau_o = 9.8566\ Ibf/100ft^2$ $\mu_p = 0.0647\ Ibf.s/100ft^2$

	30	287.4594	47.9099	0.9672	τ_o = 9.8566 Ibf/100ft^2 μ_p = 0.0647 lbf.s/100ft^2

Table 3

Sensitivity analysis of the Bingham plastic model at constant Temperature

	bingham plastic model			70^0C Temperature
Concentration g/L	RSS Ibf^2/100ft^4	RMS Ibf^2/100ft^4	R^2	Evaluated parameters
50	138.2484	23.0414	0.9626	τ_o = 9.8566 Ibf/100ft^2 μ_p = 0.0647 lbf.s/100ft^2
75	302.7926	50.4654	0.9618	τ_o = 15.3025 Ibf/100ft^2 μ_p = 0.0947 lbf.s/100ft^2
100	720.1774	120.0296	0.9672	τ_o = 20.8591 Ibf/100ft^2 μ_p = 0.1580 lbf.s/100ft^2
125	1493.3	248.8857	0.9541	τ_o = 29.9058 Ibf/100ft^2 μ_p = 0.1909 lbf.s/100ft^2

Table 1

Sensitivity analysis of the Power-law model at constant Concentration

	Power-law model			50g/L concentration
Temperature ^{0}C	RSS Ibf^2/100ft^4	RMS Ibf^2/100ft^4	R^2	Evaluated parameters
70	3.6559	0.6093	0.999	K= 1.2831 lbf.s/100ft^2 n=0.5789
60	5.7666	0.9611	0.987	K= 1.5111 lbf.s/100ft^2 n=0.5697
50	3.1803	0.5301	0.9994	K= 1.7794 lbf.s/100ft^2 n=0.5629

40	7.415	1.2358	0.9989	K= 1.7685 lbf.s/100ft^2 n=0.5786
30	5.3505	0.8917	0.9994	K= 1.6044s/100ft^2 n=0.6076

Table 2

Sensitivity analysis of the Power-law model at constant Temperature

Power-law model				70^{0}C Temperature
Concentration g/L	RSS lbf^2/100ft^4	RMS lbf^2/100ft^4	R^2	Evaluated parameters
50	3.6559	0.6093	0.999	K= 1.2831 lbf.s/100ft^2 n=0.5789
75	12.4135	2.0689	0.9984	K= 2.0729 lbf.s/100ft^2 n=0.5655
100	12.7359	2.1226	0.9994	K= 2.4644 lbf.s/100ft^2 n=0.6119
125	24.255	4.0425	0.9993	K= 4.0425 lbf.s/100ft^2 n=0.5689

Table 3

Sensitivity analysis of the Herschel-Bulkley model at constant Concentration

Herschel-Bulkley model				50g/L concentration
Temperature ^{0}C	RSS lbf^2/100ft^4	RMS lbf^2/100ft^4	R^2	Evaluated parameters
70	0.661	0.1322	0.9998	τ o= 1.6825 lbf/100ft^2 K=0.9893 lbf.s/100ft^2 n=0.6138
60	2.2883	0.4577	0.9995	τ o= 2.0336 lbf/100ft^2 K=1.1324 lbf.s/100ft^2 n=0.6085

				τ o= 1.6396 lbf/100ft^2 K=1.4561 lbf.s/100ft^2 n=0.5897
50	1.0119	0.2024	0.9998	τ o= 1.6396 lbf/100ft^2 K=1.4561 lbf.s/100ft^2 n=0.5897
40	2.0358	0.4072	0.9997	τ o= 2.0358 lbf/100ft^2 K=1.3242 lbf.s/100ft^2 n=0.6175
30	0.6807	0.1361	0.9999	τ o= 2.2074 lbf/100ft^2 K=1.2596 lbf.s/100ft^2 n=0.6403

Table 4

Sensitivity analysis of the Herschel-Bulkley model at constant Temperature

Herschel-Bulkley model				70^0C Temperature
Concentration g/L	RSS lbf^2/100ft^4	RMS lbf^2/100ft^4	R^2	Evaluated parameters
50	0.661	0.1322	0.9998	τ o= 1.6825 lbf/100ft^2 K=0.9893 lbf.s/100ft^2 n=0.6138
75	3.0026	0.6005	0.9996	τ o= 3.3595 lbf/100ft^2 K=1.4439 lbf.s/100ft^2 n=0.6142
100	2.9597	0.5919	0.9999	τ o= 3.1689 lbf/100ft^2 K=1.9776 lbf.s/100ft^2 n=0.6416
125	2.0358	0.4072	0.9997	τ o= 3.1894 lbf/100ft^2 K=3.4542 lbf.s/100ft^2 n=0.5908

Table 5

Sensitivity analysis of the Robertson-Stiff model at constant Concentration

Robertson stiff model				50g/L concentration
Temperature ^0C	RSS lbf^2/100ft^4	RMS lbf^2/100ft^4	R^2	Evaluated parameters
70	1.0001	0.2	0.9997	A= 1.1314 lbf.s$^{0.4026}$/100ft^2 B= 0.5974 γo= 5.1561s^{-1}
60	2.4003	0.4801	0.9995	A= 1.3364 lbf.s$^{0.4026}$/100ft^2 B= 0.5877 γo= 5.02071s^{-1}

50	1.2291	0.2458	0.9998	$A= 1.6428$ $lbf.s^{0.4026}/100ft^2$ $B= 0.5746$ $\gamma o= 3.1561s^{-1}$
40	2.9577	0.5915	0.9996	$A= 1.5688$ $lbf.s^{0.4026}/100ft^2$ $B= 0.5962$ $\gamma o= 4.8712s^{-1}$
30	1.2911	0.2582	0.9999	$A= 1.4448$ $lbf.s^{0.4026}/100ft^2$ $B= 0.6230$ $\gamma o= 4.3726s^{-1}$

Table 6

Sensitivity analysis of the Robertson-Stiff model at constant Temperature

	Robertson stiff model			70^0C Temperature
Concentration g/L	RSS $lbf^2/100ft^4$	RMS $lbf^2/100ft^4$	R^2	Evaluated parameters
50	1.0001	0.2	0.9997	$A= 1.1314$ $lbf.s^{0.4026}/100ft^2$ $B= 0.5974$ $\gamma o= 5.1561s^{-1}$
75	4.9243	0.9849	0.9994	$A= 1.7902$ $lbf.s^{0.4026}/100ft^2$ $B= 0.5871$ $\gamma o= 5.9465s^{-1}$
100	3.9647	0.7929	0.9998	$A= 2.2377$ $lbf.s^{0.4026}/100ft^2$ $B= 0.6260$ $\gamma o= 4.0409s^{-1}$
125	13.9958	2.7992	0.9996	$A= 3.7744$ $lbf.s^{0.4026}/100ft^2$ $B= 0.5799$ $\gamma o= 3.0094s^{-1}$

Table 7

Sensitivity analysis of the Prandtl-Eyring model at constant Concentration

	Prandtl-Eyring model			50g/L concentration
Temperature ^0C	RSS $lbf^2/100ft^4$	RMS $lbf^2/100ft^4$	R^2	Evaluated parameters
70	89.9357	14.9893	0.9757	$A=26.7032$ $B=191.6690$
60	110.5825	18.4304	0.9754	$A=28.5214$ $B=146.8925$

50	130.4108	21.7351	0.9771	A=31.3211 B=138.9497
40	170.0923	28.3487	0.9757	A=36.7871 B=159.6589
30	171.7857	28.631	0.9804	A=44.1196 B=191.6690

Table 8

Sensitivity analysis of the Prandtl-Eyring model at constant Temperature

	Prandtl-Eyring model			70^0C Temperature
Temperature ^0C	RSS $Ibf^2/100ft^4$	RMS $Ibf^2/100ft^4$	R^2	Evaluated parameters
50	89.9357	14.9893	0.9757	A=26.7032 B=191.6690
75	230.7298	38.455	0.9709	A=37.9289 B=145.7596
100	404.8721	67.4787	0.9816	A=70.7152 B=197.3360
125	613.7895	102.2982	0.9811	A=76.8097 B=148.2323

Nomenclature

A = Model parameter for Roberston-Stiff, Prandtl-Eyring fluid model

B = Model parameter for Roberston-Stiff, Prandtl-Eyring fluid model

f(γ, β) = General expression for rheological models

Matlab = Matrix Laboratory Software

M = Number of model parameters

N = Number of data points

R^2 = Coefficient of determination

RMS = Residual Mean Square in $Ibf^2/100ft^4$

RSS = Residual Sum of Square in $Ibf^2/100ft^4$

μ = value of model parameter

ε = Random error in $Ibf/100ft^2$

τ = Shear stress in $Ibf/100ft^2$

$τ_0$ = Yield stress in $Ibf/100ft^2$

$μ_p$ = Plastic viscosity, $Ibf.s/100ft^2$

γ = Shear rate in sec^{-1}

$γ_o$ = Yield shear rate

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