Jahn–Teller impurity dependence of the transition temperature $T_{c1}$, critical exponent and pseudo-Jahn–Teller potential well splitting in ZnTiF$_6$. 6H$_2$O

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Abstract. The 182 K ($\approx$91.2 °C) trigonal-to-monoclinic phase transition in ZnTiF$_6$. 6H$_2$O single crystal has been studied by EPR, for various concentrations of doped Jahn–Teller (JT) impurity Cu$^{2+}$ ions and also for non-JT impurity Ni$^{2+}$ ions. The transition temperature $T_{c1}$, which decreases with increase in impurity concentration, is more strongly affected by the JT impurity. The critical exponent $\beta$ as well as the JT potential well splitting $E_0$ have been determined from the temperature variation in EPR signal intensity in the immediate neighbourhood of $T_{c1}$ for the Cu$^{2+}$ impurity. The critical exponent $\beta$ and $E_0$ are dependent strongly on the JT impurity concentration. Two for two different concentrations of Cu$^{2+}$ ions, i.e. 0.043 wt% and 0.98 wt%, the values of $\beta$ are 0.5 ± 0.05 and 0.12 ± 0.03, respectively, while the values of $E_0$ are 140 ± 15 cm$^{-1}$ and 97 ± 13 cm$^{-1}$, respectively. The value of $E_0$ for a deuterated crystal containing a low Cu$^{2+}$ concentration is 78 ± 10 cm$^{-1}$. The decrease in $E_0$ with increasing Cu$^{2+}$ concentration for a hydrated crystal and also with deuteration (for a low copper concentration) is in qualitative agreement with the corresponding gradual phase transition observed in these materials.

1. Introduction

The crystal-zinc fluorotitanate hexahydrate: ZnTiF$_6$. 6H$_2$O (ZTFH), belongs to the class of compounds having the general formula A$_2$BF$_6$. 6H$_2$O where A = Zn, Mn, Ni, Co, Mg, etc and B = Ti, Si, Ge, etc. The structure consists of nearly regular A(H$_2$O)$_6$ and BF$_6$ octahedra packed in a trigonally distorted structure similar to that of CsCl. Many compounds of the above series exhibit first-order structural phase transitions in the temperature range 130–300 K, from the high-temperature trigonal phase (R3m) to the low-temperature monoclinic phase (P2$_1$/c) (Kodera et al 1972, Syoyama and Osaki 1972).

EPR measurements on ZTFH: Ni$^{2+}$ by Rubins (1974) indicated the loss of high-temperature axial symmetry of Zn(H$_2$O)$_6$ octahedra below 182 K and the development of six inequivalent magnetic sites, each with a rhombic component; the spectra coincide with the pseudo-trigonal C axis. $^{19}$F NMR studies (Afanasjev et al 1979) reveal a first-order phase transition at −91.2°C ($T_{c1}$) when the rotation of the fluorine octahedra freezes and the single $^{19}$F line splits into two, indicating the loss of a chemical equivalence.

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between the fluorne atoms following a tetragonal distortion of the TiF$_6^-$ octahedra. Chowdhury et al (1981) found a second weak transition of a continuous nature in ZTFH at 217 K. The latter transition is found to occur in ZnTiF$_6$ : $^{5}$D$_2$O (ZTFD) at $-43.5^\circ$C ($T_c$), where $T_c$ is not affected by deuteration. Recently, Chowdhury et al (1985) examined the temperature dependence of the Raman spectra of both ZTFH and ZTFD and found that some bands show an interesting behaviour near the transition temperature. The frequency of the symmetric stretching vibrational mode $\nu(H_2O-D_2O)$ in both ZTFH and ZTFD increases sharply by about 6 cm$^{-1}$ at the phase transition temperature as the crystal is cooled and then remains constant for the low-temperature phase. Das et al (1985) theoretically investigated the various coupling between the vibrational and rotational modes of TiF$_6^-$ and (M$^{2+}$, H$_2$O) octahedra. Chowdhury et al (1983) performed IR and Raman spectroscopy measurements and concluded that the librational modes of the water molecule change significantly around the transition temperature.

De et al (1984) performed EPR measurements on ZTFH : Cu$^{2+}$ (Cu$^{2+}$ substituting for some of the Zn sites). Cu$^{2+}$ ions in this system have an orbitally degenerate $E$ ground state and the system exhibits a strong Jahn–Teller (JT) effect as confirmed by them. The JT stabilisation energy $E_{JT} = 1000$ cm$^{-1}$ has been determined from a fit of the EPR linewidth, which varies exponentially with temperature, to an Orbach relaxation mechanism (De 1986). Further, from the gradual variation of the spin Hamiltonian parameters $g_\parallel$, $g_\perp$, $A_{JT}$ and $A_{L}$ down to 4.2 K, it has been concluded that one of the three JT potential wells is lower than the other two by an energy $E_0$ of 140 cm$^{-1}$. With a low Cu$^{2+}$ concentration of 0.043 wt% the concentration temperature was lowered by 11°C from that of pure ZTFH. $T_c$ was further lowered when the crystal was powdered.

Because of possible interaction between the soft mode driving the phase transition and the JT active modes, the JT effect in such systems is modified in comparison with those JT systems which do not exhibit any structural transition (De 1986), e.g. ZnSiF$_6$ : $^{6}$H$_2$O, MgO, CaO, La$_2$Mg$_3$(NO$_3$)$_6$, $^{2}$H$_2$O doped with Cu$^{2+}$. Another interesting observation was that the spin–lattice relaxation rate $1/T_1$ was much slower in ZTFH : Cu$^{2+}$ than in the latter systems.

In this paper, we report a systematic study of the dependence of the phase transition temperature $T_c$ on JT impurity, i.e. Cu$^{2+}$ concentration and compare it with that of non-JT impurity, i.e. Ni$^{2+}$, concentration in ZTFH. Further, we explore the dependence of the critical behaviour and the critical exponent $\beta$ on JT impurity concentrations from EPR measurements in the immediate neighbourhood of the transition temperature. From such measurements, we have been able to determine also the JT potential splitting $E_0$. The decrease in $E_0$ with increase in Cu$^{2+}$ concentration and deuteration is discussed and found to be consistent with the corresponding gradual phase transition observed in this material. Deviation from mean-field behaviour is observed for high concentrations.

2. Experimental details

Single crystals of ZTFH were grown by slow evaporation of an aqueous solution of ZnTiF$_6$ obtained by dissolving ZnCO$_3$ in 40% H$_2$TiF$_6$ : CuCO$_3$ and NiCO$_3$ were added to grow doped crystals of various concentrations. Recrystallisation was done to reduce the Mn$^{2+}$ impurity concentration beyond the detection limit in these crystals. Unlike Cu$^{2+}$ and Ni$^{2+}$, Mn$^{2+}$ in these crystals produces a slight raising of $T_c$. Only good single crystals devoid of any twinning and with uniform concentrations of Cu$^{2+}$ were chosen for the experiments. These crystals were analysed by Galbraith Chemical Laboratories, USA,
Estimation of the impurity concentration. For the phase transition study, EPR spectra were measured in the (110) plane of the crystal with the magnetic field direction along the $g_{\text{ax}}$ (this direction is close to the $g_1$ direction or [100] direction of the Cu$^{2+}$ ion and corresponds to the maximum $g$ value in the (110) plane). Accuracy of determining the onset of phase transition is higher in this direction because of the appearance of as many as six lines with the largest field separations (De et al. 1984).

Above $T_s$, the EPR spectrum consists of an isotropic line only. It may be mentioned that it is not possible to determine the phase transition along the [111] direction because all the EPR lines remain coincident even after phase transition except for the appearance of four copper hyperfine lines at around 120 K. The EPR spectrometer used was a Q-band (33–35 GHz) reflectance spectrometer built in the laboratory. Temperatures were varied by a manual control. An approximately uniform cooling and heating rate of between 1 °C min$^{-1}$ and 1 °C per 120 min could be attained. The sample could be maintained at any temperature above 77 K (liquid-N$_2$ temperature) to within ±0.1 °C for 30 min. The temperature of the sample structure was measured by both E- and T-type thermocouples. The thermometers and the digital readouts were calibrated at the temperatures of liquid N$_2$, solid CO$_2$, a toluene-and-liquid-N$_2$ slush and a mixture of isopropanol and solid CO$_2$.

3. Enhanced lowering of the phase-transition temperature $T_{el}$

The transition temperature $T_{el}$ was recorded through the variation in the intensity $I$ of the isotropic signal as the sample was cooled at a uniform rate of 3 °C h$^{-1}$. Increases up to about 1 °C above the phase transition. The sample is then cooled at a rate of 0.5 °C h$^{-1}$.

$T_f$ during cooling can be noted by the appearance of the high-field lines or by a noticeable reduction in the isotropic EPR signal intensity $I$ (as high as 60% in dilute material; see figures 1 and 5) with a temperature variation of ±0.1 °C. In figure 1, it can be seen that at −102.6 °C there is a noticeable change in $I$ from that at −102.5 °C. This is associated with the appearance of high-field signals which is prominent at −102.7 and −102.8 °C. So $T_e$ for a Cu$^{2+}$ concentration of 0.043 wt% could be recorded as −102.6 ± 0.2 °C (±0.1 °C is the error in the temperature recording). It can be seen that both the high- and the low-temperature phases coexist over a finite temperature interval $\Delta T$. $\Delta T$ is found to be concentration dependent. The isotropic signal vanishes a few degrees Celsius below $T_{el}$. The anisotropic signals gain intensity as the sample is cooled. Hyperfine

![Figure 1: EPR spectra of ZTPH: Cu$^{2+}$ recorded in the immediate neighbourhood of the phase transition temperature $T_{el}$ for a Cu$^{2+}$ concentration of 0.043 wt%.

\[ T \ (°C) \]

-102.3
-102.5
-102.6
-102.7
-102.8
-103.2
-105.0
-115.9

\[ \Delta T \]
structure appears at around 118 K. Both the $g$- and the $A$-values are temperature dependent down to 4.2 K.

During warming from the low-temperature phase, the transition is noticed by changes taking place in the reverse order. However, the transition temperature $T_{c1}$ ↑ during warming from the low-temperature phase is slightly higher than the transition temperature $T_{c1}$ ↓ during cooling from the trigonal phase. The decreases $\Delta T_c$ in $T_{c1}$ ↑ and $T_{c1}$ ↓ from the transition temperature $T_{c0}$ of pure ZTFH for different concentrations are shown in figures 2 and 3. The decrease $\Delta T_c$ in $T_{c1}$ from that of $T_{c0}$ increases with both Cu$^{2+}$ and Ni$^{2+}$. It is significantly higher for Cu$^{2+}$ JT impurity than for Ni$^{2+}$ (non-JT impurity) for the same concentration. The value of the transition temperature $T_{c1}$ obtained is independent of the orientation of the crystal. The observed enhanced lowering of $T_{c1}$ for a JT impurity in comparison with that for a non-JT impurity will be explained in a later paper.

4. Critical phenomena

As discussed earlier, the EPR signal intensity varies sharply in the neighbourhood of $T_{c1}$ for low Cu$^{2+}$ concentrations (the neighbourhood may be as small as 0.1 °C). However, as the Cu$^{2+}$ concentration is increased, the transition is found to become gradual with respect to temperature (figure 4). The temperature interval $\Delta T$ over which both the phases coexist (trigonal R3m and monoclinic phases $P2_1/c$) widens with increase in the Cu$^{2+}$ concentration. A high Cu$^{2+}$ impurity concentration thus drives the phase transition
Figure 3. Decrease in the transition temperature $T_\text{c1}$ from $T_\text{c0}$ of pure ZTFH, due to the addition of Ni$^{2+}$ impurities: ●, on warming; ■, on cooling.

Figure 4. The EPR spectrum recorded for a Cu$^{2+}$ concentration of 3.7 wt% in ZTFH. It is seen that the transition to the monoclinic phase (see text) takes place gradually with respect to the change in temperature in contrast with the sharp transition observed for low Cu$^{2+}$ concentrations (see figure 1).
towards continuous or higher order (compare figures 1 and 4). To investigate the
of the phase transition and the critical behaviour for two different concentra-
ions, i.e. 0.043 wt% and 0.98 wt%, we have recorded the EPR signal intensity
the sample is cooled or warmed at a rate of 0.5°C per 100 min, every 0.1°C (dT) intervals
around the phase transition. At a given temperature the sample is maintained for a long
time to ensure that no further change in EPR signal intensity takes place. dT/Tc is about
5 x 10^-4 and therefore the critical phenomena can be studied from such measurements.
The plot of normalised intensity I with temperature thus recorded is shown in figures
S(a) and 6(a). Figures 5(b) and 6(b) show the plots of log (I/I_m) versus log ε, where ε =
|1 - T/T_c| 1. In figure 5(b), T_m corresponds to the transition at the point A. Three points
on this plot which are obtained for the points A, B, C and D in figures 5(a) (where the
temperature differences between the point A and the points B, C and D are taken to be
0.1°C, 0.2°C and 0.3°C, respectively) lie in a straight line with a slope β of 0.5 ± 0.05,
for the Cu + concentration 0.043%. Thus, for this low concentration, mean-field-type
behaviour is observed. However, for the higher Cu + concentration (0.98 wt%), the plot
(figure 6(b), line 1) for the points A, B, C, D and E is shown by full circles and a full line
to guide the eye (here, the temperature differences between the point A and the points
B, C, D and E are taken to be 0.1°C, 0.2°C 0.3°C and 0.4°C, respectively). T_m
corresponds to the minimum intensity observed at the transition corresponding to the
point A. The corresponding slope β of the line is 0.17 ± 0.05. However, if we take the
exact temperature differences between the point A and the points C, D and E as shown
in the graph, we obtain the plot (figure 6(b), 2) shown by the three circles with dots in.
The corresponding slope β of the straight line passing through these points is 0.12 ± 0.03.
The EPR signal intensity I may be related to the order parameter of the phase transition,
which is related to the orientation and tetragonal distortion of the TiF_4^2- group at the
transition (Bose et al. 1983, Afanasyev et al. 1979) and β may be taken as the critical
exponent in the relation I/I_m = e^-β. As determined in this experiment, the value of β
lies between 0.17 and 0.12 for the 0.98 wt% Cu + concentration; however, the preferred

Figure 5. (a) The plot of the normalised isotropic EPR signal intensity (normalised with
respect to the maximum EPR intensity immediately before the transition starts) with tem-
perature change in the immediate neighbourhood of Tc while cooling from the high-
temperature phase (the Cu + concentration in ZnF_2 is 0.043 wt%); (b) the plot of log ε versus
log(I/I_m) (see text).
value is 0.12. Thus, we see that, with a high JT impurity concentration, there is a deviation from mean-field behaviour. This feature is under further study using different Cu$^{2+}$ concentrations and Ni$^{2+}$ concentrations in ZTFH as well as in ZTFD.

5. The Jahn-Teller potential splitting

The sharp drop in the isotropic EPR signal intensity $I$ may be related to the JT potential splitting $E_0$. From our earlier work on JT systems of ZTFH: Cu and MgSiF$_6$·6H$_2$O: Cu (Rubins et al 1984), it is established that the three JT potential wells (corresponding to JT distortions along the $x$, $y$, $z$ axes of the [Cu$^{2+}$·6H$_2$O] complex are equivalent in the trigonal phase (figure 7(a))).

Figure 7. Schematic picture showing that the JT potential wells are non-equivalent by an energy $E_0$ below $T_{c1}$. 
However, below $T_{el}$, i.e. in the monoclinic phase, the wells are non-equiva
taneous energy $E_0$ (figure 7(b)). The energy $E_0$ has been determined previously (De, 1984) for very low Cu$^{2+}$ concentrations (0.043 wt%) from temperature variations in the spin Hamiltonian parameters $g_1, g_2, A_1$ and $A_2$ down to 4.2 K. It should be noted that $E_0$ is not the same as the JT stabilisation energy $E_{JT}$.

In the following, we show that it is also possible to determine $E_0$ from the observed abrupt drop in EPR intensity at $T_{el}$. When the sample is cooled from the high-temperature phase, we assume that, at $T_{el}$, one of the three JT potential wells becomes lower than the other two by an energy $E_0$ (figure 7(b)), i.e. the initial splitting occurs at $T_{el}$ although, below $T_{el}$, $E_0$ may increase with decrease in temperature. The energy separation between the other two wells is much smaller than $E_0$ and we neglect it in the following calculations. It should be noted that these three wells are actually warped and the minima are separated by 120°, 240° in the plane of $Q_0$, $Q_y$; $Q_0$, $Q_y$ are the normal coordinates of the complex transforming as $dx^2, dy^2$ and $dx^2-\eta y^2$ of 3d$^9$ wavefunctions. The isotropic EPR signal in a JT system in general is due to rapid tunnelling or phonon-induced reorientation among the three wells; it may also arise because of the population of the vibronic levels $^{2}A_2$ or $^{2}A_1$ (Ham 1971). In ZnTFH: Cu$^{2+}$, the populated level $^{2}A_1$ level seems to give rise to the isotropic signal (De 1986).

When the measurement is made along one of the three [100] directions, the EPR signal intensity is proportional to the ground-state population of the $^{2}A_2$ state in one of the wells in figure 7(a), i.e. for $T = T_{el} + \delta$

$$\lim_{T \to T_{el}^-} I_{el} = \frac{1}{CN_0}. \quad (1)$$

$C$ is the proportionality constant. $N_0$ is the total population of the $^{2}A_2$ state in the three wells at $T_{el}$. This is based on the fact that the tunnelling frequency is smaller than the microwave frequency. Otherwise, the factor $1$ in equation (1) should be omitted. It may be mentioned that the spin–lattice relaxation rate $1/T_1$ calculated from equation (6) of the paper by De (1986) is found to be about $6 \times 10^6$ s$^{-1}$, $1/T_1$, which includes contribution from the phonon-induced reorientation and tunnelling among the three JT wells, is much smaller in the present system than in JT systems (see §1) exhibiting no structural transition (De 1986). Using the approximate $R$ value found by Dang et al. (1974) of $(1/T_1)/(1/T_1) = 6.4 \times 10^{-3}$ for the (100) orientation in ZnSiF$_6.6$H$_2$O: Cu$^{2+}$, we can approximately estimate the value of the tunnelling rate $1/T_1$ at $T_{el}$ in ZnTFH: Cu$^{2+}$ to be $0.94 \times 10^6$ s$^{-1}$, much less than the microwave frequency of 35 GHz employed in this work. Below the transition point $T_{el}$, the population distributions in the three wells as described in figure 7(b) are as follows:

$$N_2 = N_1 \exp(-E_0/kT). \quad (2)$$

$$N_1 + 2N_2 = N_0 \quad (3)$$

Thus,

$$N_1 = N_0 \exp(-E_0/kT)/(1 + 2\exp(-E_0/kT)). \quad (4)$$

Tunnelling may still be present among these wells. However, now $N_1$ corresponds to the anisotropic EPR signal because, with a lowering of the temperature below $T_{el}$, $N_1$ increases at the expense of $N_2$. This is reflected in the observed increase in anisotropic signal intensities at the expense of the isotropic signal intensity. So, we can say that the isotropic signal intensity $I$ immediately below the transition still corresponds to the
II impurity dependence of $T_{c1}$, $\beta$ and $E_0$ in ZnTiF$_6\cdot6$H$_2$O

Excitation $N_2$ of the $^2A_2$ state in one of the two upper wells and we have

$$\lim_{\omega \to 0} (I_{T_{c1}-\omega}) = CN_2.$$  \hspace{1cm} (5)

Thus, from equations (1), (4) and (5), we obtain

$$r = \lim_{\omega \to 0} (I_{T_{c1}-\omega}/I_{T_{c1}+\omega}) = 3x/(1 + 2x)$$  \hspace{1cm} (6)

where $x = \exp(-E_0/kT_{c1})$. Equation (6) tells us that, if $E_0 = 0$ at $T_{c1}$, we expect continuous transition. If $E_0 = \infty$ at the transition, we expect ideal abrupt transition. For intermediate $E_0$, we expect transitions whose nature lies between `ideal continuous' and `ideal abrupt'.

Let us see how this model allows us to evaluate $E_0$ from the observed variations in the isotropic signal intensity $I$ in figures 5 and 6 for Cu$^{2+}$ concentrations of 0.043 and 0.98 wt% in ZTFH. We determine from these figures that the corresponding values of $r$ are $0.56 \pm 0.04$ and $0.70 \pm 0.05$, with the corresponding transition temperatures $T_{c1}$ being $171.5$ K and $164.5$ K, respectively. We then determine from equation (6) that the corresponding values of $E_0$ are $140 \pm 14$ cm$^{-1}$ and $94 \pm 11$ cm$^{-1}$, respectively. This means that for higher concentrations the splitting $E_0$ will decrease. From equations (4) and (5), below $T_{c1}$ but for temperatures close to $T_{c1}$, $z = (dI/dT)/I \propto E_0/kT_{c1}(1 + 2x)$ where we neglect terms such as $\exp(-\mu_0 H/kT)$, which is important only at low temperatures (less than 4.2 K). $z$ decreases with decrease in $E_0$, which means that, as $E_0$ decreases with increase in Cu$^{2+}$ concentration, the transition may become gradual with respect to temperature. The observed gradual transition (gradual in the sense that the isotropic signal due to the trigonal phase of ZTFH continues to exist over a finite temperature interval, which increases with increasing Cu$^{2+}$ concentration) for high Cu$^{2+}$ concentrations (figure 4) is thus consistent with the above model.

6. Effect of deuteration

We have repeated the above experiment and analysis for a ZTFD crystal containing a low Cu$^{2+}$ concentration. The transition is found to be gradual with respect to temperature as seen from figure 8, unlike the hydrated crystal containing a low Cu$^{2+}$ concentration. $T_{c1}$ may be noted to be $-105.5$°C where there is clearly a significant change in the isotropic signal intensity from that at $-105$°C. This is accompanied by the appearance of signals (anisotropic) on the high-field side as well as on the low-field side. The value of $r$ in equation (6) may be taken to be the ratio in figure 8 of the EPR intensities at $-105.5$ and $-105$°C, $r$ is determined to be $0.78 \pm 0.017$. With $T_{c1} = 167$ K, we then obtain from equation (6) that $E_0 = 77 \pm 9$ cm$^{-1}$. This value of $E_0$ is consistent with the gradual transition observed in this crystal. An experimental study on the critical behaviour in the deuterated crystal containing different Cu$^{2+}$ and Ni$^{2+}$ concentrations is in progress. If the same correlation exists in the deuterated crystal, then we should expect decreasing values of the critical exponent $\beta$ and the splitting of $E_0$ with increasing Cu$^{2+}$ concentration. Moreover, the value of the critical exponent in the deuterated crystal for a given Cu$^{2+}$ concentration should be smaller than that in the hydrated crystal. In general, a smaller critical exponent means that the dimensionality of the system at the phase transition is low, and gradual or continuous transitions can be expected.
Figure 8. EPR spectrum of Cu$^{2+}$ in ZTFD showing that deuteration changes the nature of the phase transition from abrupt to gradual (compare with figure 1 and see text). The $E_0$ value is much lower than that of the hydrated crystal.

7. Conclusion

The origin of $E_0$ may be said to lie in the monoclinic distortion of the host lattice, i.e., ZTFD at $T_c$. So $E_0$ is a measure of the distortion. For no structural transition, $E_0$ should be zero or very small. The fact that $E_0$ as well as $\beta$ are smaller for higher JT impurity concentrations might mean that the higher JT impurity concentration is offering resistance to the lattice from undergoing a structural transition. Physically, this means that $T_c$, the temperature at which the soft mode frequency of the system becomes zero, is strongly dependent on the presence of a JT impurity, indicating a coupling of the soft mode to the JT modes. Since the sharp transition at $T_{c1}$ is associated with the tetragonal distortion of the TiF$_4^{2-}$ octahedra (Chowdhury et al. 1981, 1985) and the weak continuous transition at $-56 \,^\circ C$ is associated with the tilt of the [M$^{2+}$, H$_2$O] octahedra, and since the high Cu$^{2+}$ concentration tends to make the transition at $T_{c2}$ continuous or gradual, it is possible that the JT impurity concentration is influencing the coupling of the modes associated with these two units which constitute the crystal ZTFD in a CsCl packing. It should be noted that in pure ZTFD the transition at $T_{c2}$ ($-43 \,^\circ C$) is of a more continuous nature than that of pure ZTFH. At $T_{c3}$ the tilt of the water octahedra constitutes the soft mode. When this is combined with our observation of gradual transition at $T_{c1}$ in ZTFD even for low Cu$^{2+}$ concentrations, we also see that coupling of the above two modes via a JT impurity is possible. However, the fundamental questions of how the JT effect influences the said coupling and the dimensionality of phase transition in this crystal remain to be theoretically investigated. It is also not understood whether the decrease in transition temperature $T_{c2}$ in powdered material (containing a low Cu$^{2+}$ concentration (De 1986)) has the same underlying cause as the decrease in $T_{c1}$ in crystals containing a high Cu$^{2+}$ concentration. It may appear that in powdered material the short-range correlation of the soft mode rather than the long-range correlation would be predominant, while in single crystals with high Cu$^{2+}$ concentrations the soft mode would
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It is expected to have long-range correlation, because of the possible interaction between the soft mode and the JT active modes (Hock and Thomas 1977). Determinations of the critical exponent and the JT potential splitting $E_0$ for many different Cu$^{2+}$ and Ni$^{2+}$ concentrations in hydrated and deuterated crystals are necessary before we can throw sufficient light on the separate role of JT and non-JT impurities in the dynamics of structural transition and the above apparent contradiction in this material. Raman scattering and JT studies will be of additional help to elucidate the interaction of the different modes associated with the $[M, H_2O]^{2-}$ and $\text{TiF}_6^{2-}$ at the transition (Chowdhury et al 1983). Further useful studies will concern the application of uniaxial stress and study the changes in transition temperatures, the critical exponent and the JT splitting $E_0$.

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